

Data Management

08 Query Processing

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Query Optimization and Query Processing

```
SELECT * FROM TopScorer
WHERE Count >= 4
```

```
CREATE VIEW TopScorer AS
SELECT P.Name, Count(*)
FROM Players P, Goals G
WHERE P.Pid=G.Pid
AND G.GOwn=FALSE
GROUP BY P.Name
ORDER BY Count(*) DESC
```

WHAT



Yes, but **HOW** to
we get there
efficiently

Name	Count
James Rodríguez	6
Thomas Müller	5
Robin van Persie	4
Neymar	4

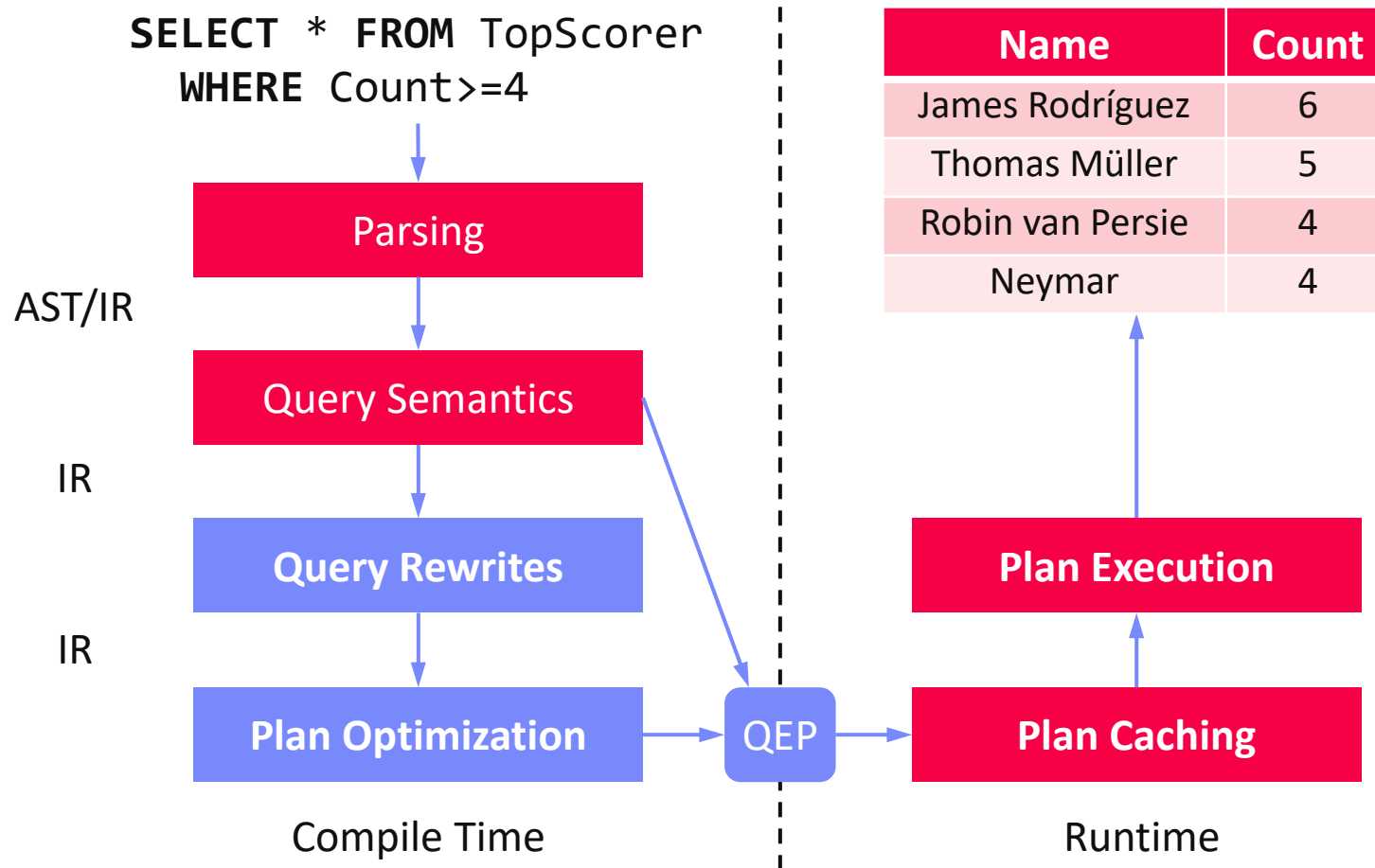
- **Goal: Basic Understanding of Internal Query Processing**
 - Query rewriting and query optimization
 - Query processing and physical plan operators
 - ➔ **Performance debugging & reuse of concepts and techniques**
 - ➔ Overview, detailed techniques discussed in **ADBS**

Agenda

- **Query Rewriting and Optimization**
- **Plan Execution Strategies**
- **Physical Plan Operators**

Query Rewriting and Optimization

Overview Query Optimization



Query Rewrites

■ Query Rewriting

- Rewrite query into semantically equivalent form that may be **processed more efficiently** or **give the optimizer more freedom**
- **#1 Same query can be expressed differently**, prevent hand optimization
- **#2 Complex queries may have redundancy**

■ A Simple Example

- Catalog meta data:
custkey is unique

```
SELECT DISTINCT custkey, name
FROM TPCH.Customer
```



```
SELECT custkey, name
FROM TPCH.Customer
```

■ 20+ years of experience on query rewriting

[**Hamid Pirahesh**, T. Y. Cliff Leung, Waqar Hasan:
A Rule Engine for Query Transformation in
Starburst and IBM DB2 C/S DBMS. **ICDE 1997**]



Standardization and Simplification

Normal Forms of Boolean Expressions

- **Conjunctive** normal form $(P_{11} \text{ OR } \dots \text{ OR } P_{1n}) \text{ AND } \dots \text{ AND } (P_{m1} \text{ OR } \dots \text{ OR } P_{mp})$
- **Disjunctive** normal form $(P_{11} \text{ AND } \dots \text{ AND } P_{1q}) \text{ OR } \dots \text{ OR } (P_{r1} \text{ AND } \dots \text{ AND } P_{rs})$

Transformation Rules for Boolean Expressions

Rule Name	Examples
Commutativity rules	$A \text{ OR } B \Leftrightarrow B \text{ OR } A$ $A \text{ AND } B \Leftrightarrow B \text{ AND } A$
Associativity rules	$(A \text{ OR } B) \text{ OR } C \Leftrightarrow A \text{ OR } (B \text{ OR } C)$ $(A \text{ AND } B) \text{ AND } C \Leftrightarrow A \text{ AND } (B \text{ AND } C)$
Distributivity rules	$A \text{ OR } (B \text{ AND } C) \Leftrightarrow (A \text{ OR } B) \text{ AND } (A \text{ OR } C)$ $A \text{ AND } (B \text{ OR } C) \Leftrightarrow (A \text{ AND } B) \text{ OR } (A \text{ AND } C)$
De Morgan's rules	$\text{NOT } (A \text{ AND } B) \Leftrightarrow \text{NOT } (A) \text{ OR } \text{NOT } (B)$ $\text{NOT } (A \text{ OR } B) \Leftrightarrow \text{NOT } (A) \text{ AND } \text{NOT } (B)$
Double-negation rules	$\text{NOT}(\text{NOT}(A)) \Leftrightarrow A$
Idempotence rules	$A \text{ OR } A \Leftrightarrow A$ $A \text{ AND } A \Leftrightarrow A$ $A \text{ OR } \text{NOT}(A) \Leftrightarrow \text{TRUE}$ $A \text{ AND } \text{NOT } (A) \Leftrightarrow \text{FALSE}$ $A \text{ AND } (A \text{ OR } B) \Leftrightarrow A$ $A \text{ OR } (A \text{ AND } B) \Leftrightarrow A$ $A \text{ OR } \text{FALSE} \Leftrightarrow A$ $A \text{ OR } \text{TRUE} \Leftrightarrow \text{TRUE}$ $A \text{ AND } \text{FALSE} \Leftrightarrow \text{FALSE}$

Standardization and Simplification, cont.

- **Elimination of Common Subexpressions**

- $(A_1=a_{11} \text{ OR } A_1=a_{12}) \text{ AND } (A_1=a_{12} \text{ OR } A_1=a_{11}) \rightarrow A_1=a_{11} \text{ OR } A_1=a_{12}$

- **Propagation of Constants**

- $A \geq B \text{ AND } B = 7 \rightarrow A \geq 7 \text{ AND } B = 7$

- **Detection of Contradictions**

- $A \geq B \text{ AND } B > C \text{ AND } C \geq A \rightarrow A > A \rightarrow \text{FALSE}$

- **Use of Constraints**

- A is primary key/unique: $\pi_A \rightarrow$ no duplicate elimination necessary
 - Rule $\text{MAR_STATUS} = \text{'married'} \rightarrow \text{TAX_CLASS} \geq 3$:
 $(\text{MAR_STATUS} = \text{'married'} \text{ AND } \text{TAX_CLASS} = 1) \rightarrow \text{FALSE}$

- **Elimination of Redundancy**

- $R \bowtie R \rightarrow R, \quad R \cup R \rightarrow R, \quad R - R \rightarrow \emptyset$
 - $R \bowtie (\sigma_p R) \rightarrow \sigma_p R, \quad R \cup (\sigma_p R) \rightarrow R, \quad R - (\sigma_p R) \rightarrow \sigma_{\neg p} R$
 - $(\sigma_{p_1} R) \bowtie (\sigma_{p_2} R) \rightarrow \sigma_{p_1 \wedge p_2} R, \quad (\sigma_{p_1} R) \cup (\sigma_{p_2} R) \rightarrow \sigma_{p_1 \vee p_2} R$

Query Unnesting

[Won Kim: On Optimizing an SQL-like Nested Query. *ACM Trans. Database Syst.* 1982]



Case 1: Type-A Nesting

- Inner block is not correlated and computes an aggregate
- Solution:** Compute the aggregate once and insert into outer query

```
SELECT OrderNo FROM Order
WHERE ProdNo =
  (SELECT MAX(ProdNo)
   FROM Product WHERE Price<100)
```



```
$X = SELECT MAX(ProdNo)
      FROM Product WHERE Price<100
SELECT OrderNo FROM Order
WHERE ProdNo = $X
```

Case 2: Type-N Nesting

- Inner block is not correlated and returns a set of tuples
- Solution:** Transform into a symmetric form (via join)

```
SELECT OrderNo FROM Order
WHERE ProdNo IN
  (SELECT ProdNo
   FROM Product WHERE Price<100)
```



```
SELECT OrderNo
FROM Order O, Product P
WHERE O.ProdNo = P.ProdNo
AND P.Price < 100
```

Query Unnesting, cont.

[Won Kim: On Optimizing an SQL-like Nested Query. *ACM Trans. Database Syst.* 1982]



Case 3: Type-J Nesting

- Un-nesting of correlated sub-queries w/o aggregation

```
SELECT OrderNo FROM Order O
WHERE ProdNo IN
  (SELECT ProdNo FROM Project P
   WHERE P.ProjNo = O.OrderNo
        AND P.Budget > 100,000)
```



```
SELECT OrderNo
FROM Order O, Project P
WHERE O.ProdNo = P.ProdNo
   AND P.ProjNo = O.OrderNo
   AND P.Budget > 100,000
```

Case 4: Type-JA Nesting

- Un-nesting of correlated sub-queries w/ aggregation

```
SELECT OrderNo FROM Order O
WHERE ProdNo IN
  (SELECT MAX(ProdNo)
   FROM Project P
   WHERE P.ProjNo = O.OrderNo
        AND P.Budget > 100,000)
```



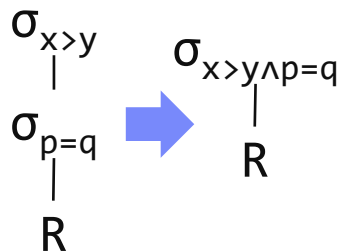
```
SELECT OrderNo FROM Order O
WHERE ProdNo IN
  (SELECT ProdNo FROM
   (SELECT ProjNo, MAX(ProdNo)
    FROM Project
    GROUP BY ProjNo) P
   WHERE P.ProjNo = O.OrderNo
        AND P.Budget > 100.000)
```

- Further un-nesting via case 3 and 2

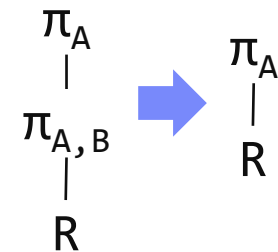
Selections and Projections

Example Transformation Rules

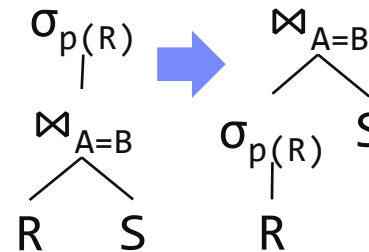
1) Grouping of Selections



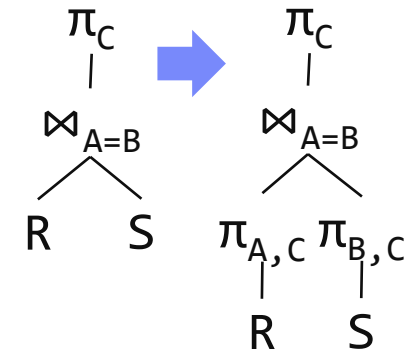
2) Grouping of Projections



3) Pushdown of Selections



4) Pushdown of Projections



Restructuring Algorithm

- #1 Split n-ary joins into binary joins
- #2 Split multi-term selections
- #3 Push-down selections as far as possible
- #4 Group adjacent selections again
- #5 Push-down projections as far as possible

Input: Standardized, simplified, and un-nested query graph

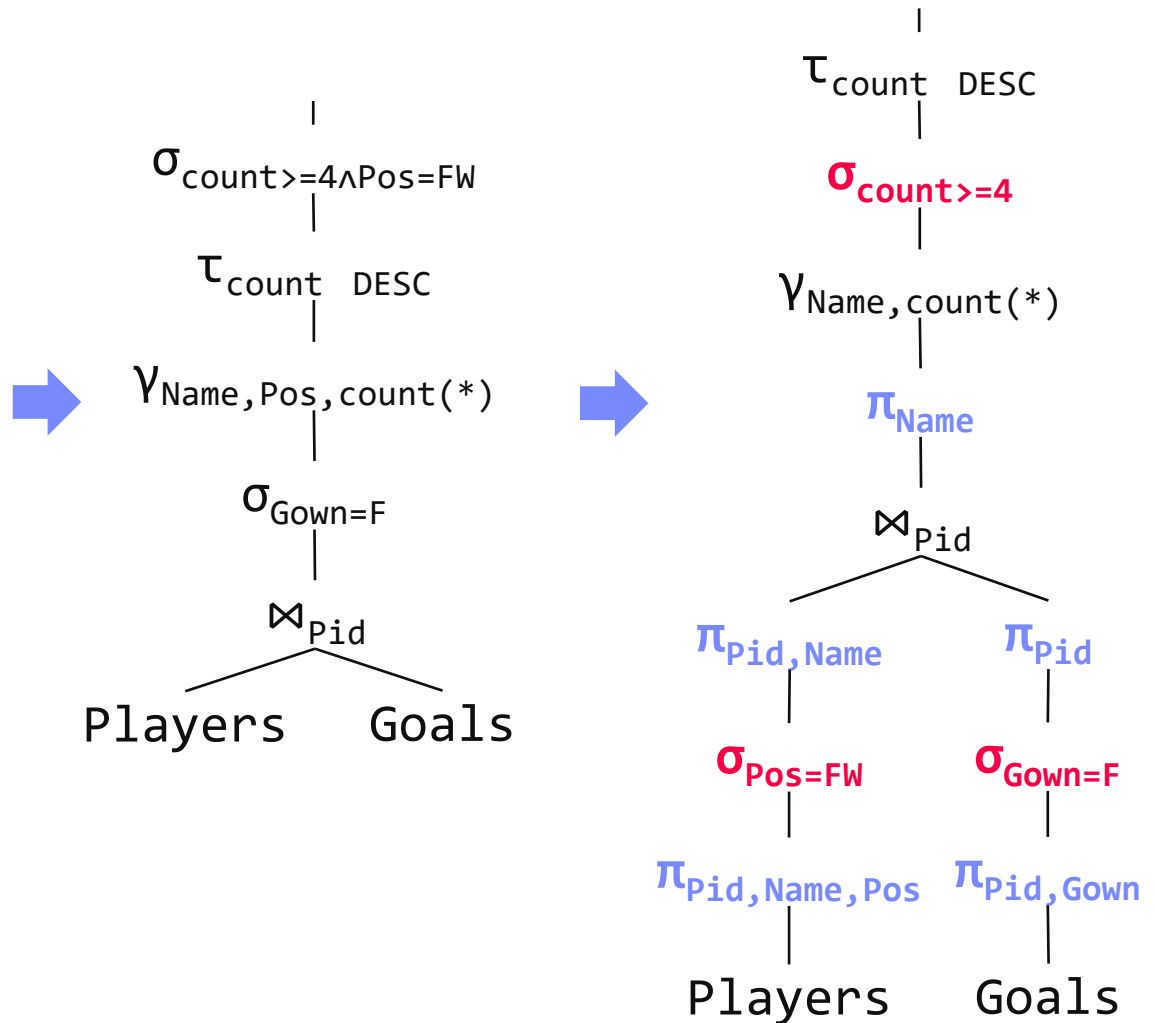
Output: Restructured query graph

Example Query Restructuring

```
SELECT * FROM TopScorer
WHERE count >= 4
AND Pos = 'FW'
```

```
CREATE VIEW TopScorer AS
SELECT P.Name, P.Pos, count(*)
FROM Players P, Goals G
WHERE P.Pid=G.Pid
AND G.GOwn=FALSE
GROUP BY P.Name, P.Pos
ORDER BY count(*) DESC
```

Additional metadata:
P.Name is unique



Plan Optimization Overview

Plan Generation

- Selection of **physical access path and plan operators**
- Selection of **execution order** of plan operators
- **Input:** logical query plan → **Output:** optimal physical query plan
- Costs of query optimization should not exceed yielded improvements

Different Cost Models

- Relies on statistics (cardinalities, selectivities via histograms + estimators)
- Operator-specific and general-purpose cost models

$$C_{\text{out}}(T) = \begin{cases} 0 & \text{if } T \text{ is a single relation} \\ |T| + C_{\text{out}}(T_1) + C_{\text{out}}(T_2) & \text{if } T = T_1 \bowtie T_2 \end{cases} \quad \text{(estimated) (real)}$$

- **I/O costs** (number of read pages, tuples)
- **Computation costs** (CPU costs, path lengths)
- **Memory** (temporary memory requirements)
- **Beware assumptions of optimizers**
(no skew, independence, no correlation)

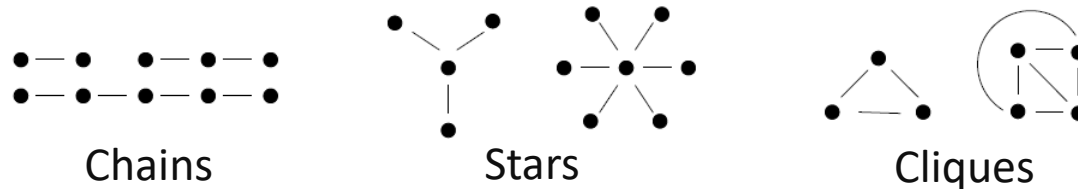
		10	590
	σ _{Model='Golf'}		
		1,000	5,000
	σ _{Make='VW'}		
Cars		10,000	10,000

Join Ordering Problem

■ **Join Ordering**

- Given a join query graph, find the optimal join ordering
- In general, **NP-hard**; but polynomial algorithms exist for special cases

■ **Query Types**



■ **Search Space**

	Chain (no CP)			Star (no CP)		Clique / CP (cross product)		
	left-deep	zig-zag	bushy	left-deep	zig-zag/ bushy	left-deep	zig-zag	bushy
n	2^{n-1}	2^{2n-3}	$2^{n-1}C(n-1)$	$2(n-1)!$	$2^{n-1}(n-1)!$	$n!$	$2^{n-2}n!$	$n! C(n-1)$
5	16	128	224	48	384	120	960	1,680
10	512	~131K	~2.4M	~726K	~186M	~3.6M	~929M	~17.6G

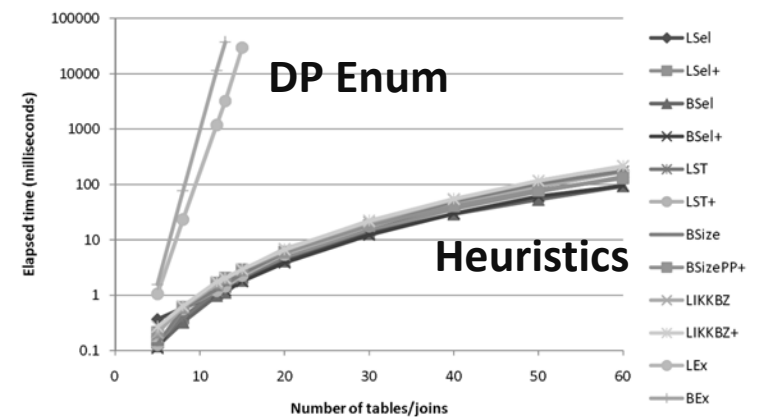
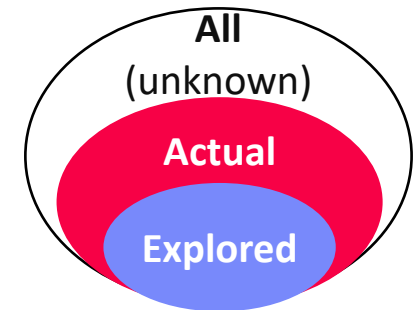
C(n) ... Catalan Numbers



[Guido Moerkotte, Building Query Compilers (Under Construction), 2019, <http://pi3.informatik.uni-mannheim.de/~moer/querycompiler.pdf>]

Join Order Search Strategies

- **Tradeoff: Optimal (or good) plan vs compilation time**
- **#1 Naïve Full Enumeration**
 - Infeasible for reasonably large queries (long tail up to 1000s of joins)
- **#2 Exact Dynamic Programming**
 - Guarantees optimal plan, often too expensive (beyond 20 relations)
 - Bottom-up vs top-down approaches
- **#3 Greedy / Heuristic Algorithms**
- **#4 Approximate Algorithms**
 - E.g., Genetic algorithms, simulated annealing
- **Example PostgreSQL**
 - Exact optimization (DPSize) if < 12 relations (geqo_threshold)
 - Genetic algorithm for larger queries
 - Join methods: NLJ, SMJ, HJ

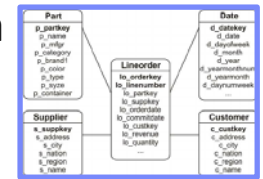


[Nicolas Bruno, César A. Galindo-Legaria, Milind Joshi: Polynomial heuristics for query optimization. **ICDE 2010**]



Greedy Join Ordering

Star Schema Benchmark



■ **Example**

- Part ⋈ Lineorder ⋈ Supplier ⋈ σ(Customer) ⋈ σ(Date), **left-deep plans**

#	Plan	Costs
1	Lineorder ⋈ Part	30M
	Lineorder ⋈ Supplier	20M
	Lineorder ⋈ σ(Customer)	90K
	Lineorder ⋈ σ(Date)	40K
	Part ⋈ Customer	N/A

2	(Lineorder ⋈ σ(Date)) ⋈ Part	150K
	(Lineorder ⋈ σ(Date)) ⋈ Supplier	100K
	(Lineorder ⋈ σ(Date)) ⋈ σ(Customer)	75K

3	((Lineorder ⋈ σ(Date)) ⋈ σ(Customer)) ⋈ Part	120K
	((Lineorder ⋈ σ(Date)) ⋈ σ(Customer)) ⋈ Supplier	105M
4	((((Lineorder ⋈ σ(Date)) ⋈ σ(Customer)) ⋈ Supplier) ⋈ Part)	135M

Note: Simple O(n²) algorithm for left-deep trees; O(n³) algorithms for bushy trees existing (e.g., GOO)

Dynamic Programming Join Ordering

▪ **Exact Enumeration via Dynamic Programming**

- #1: **Optimal substructure** (Bellman’s Principle of Optimality)
 - #2: **Overlapping subproblems** allow for memoization
- ➔ Approach DPSize: Split in independent subproblems (optimal plan per set of quantifiers and interesting properties), solve subproblems, combine solutions

▪ **Example**

Q1	Plan
{C}	Tbl, IX
{D}	Tbl, IX
{L}	...
{P}	...
{S}	...

Q2	Plan
{C,L}	L⋈C, C⋈L
{D,L}	L⋈D, D⋈L
{L,P}	L⋈P , P⋈L
{L,S}	L⋈S , S⋈L
{C,D}	N/A
...	...

Q3	Plan
{C,D,L}	(L⋈C)⋈D, D⋈(L⋈C) , (L⋈D)⋈C, C⋈(L⋈D)
{C,L,P}	(L⋈C)⋈P, P⋈(L⋈C), (P⋈L)⋈C, C⋈(P⋈L)
{C,L,S}	...
{D,L,P}	...
{D,L,S}	...
{L,P,S}	...

Q4	Plan
{C,D,L,P}	((L⋈C)⋈D)⋈P , P⋈((L⋈C)⋈D)
{C,D,L,S}	...
{C,L,P,S}	...
{D,L,P,S}	...

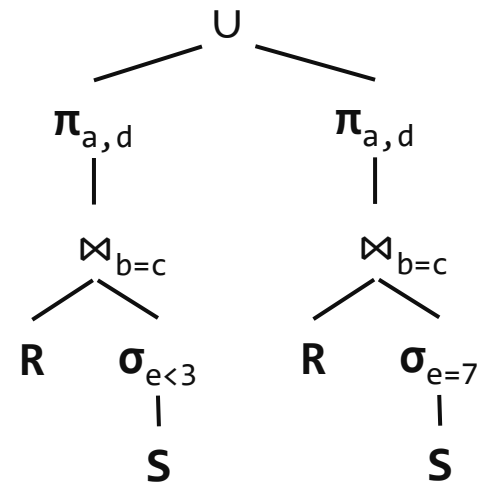
Q5	Plan
{C,D,L,P,S}	...

BREAK (and Test Yourself)

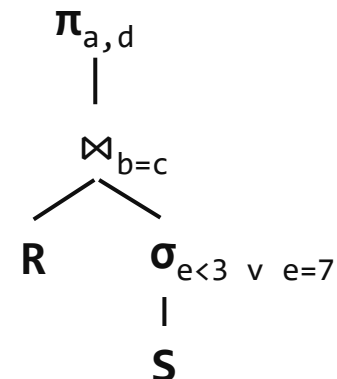
- Assume tables $R(a,b)$ and $S(c,d,e)$, draw a logical query tree in relational algebra for the following query (5/100 points)

```

SELECT R.a, S.d
  FROM R, S
 WHERE R.b = S.c AND S.e < 3
UNION ALL
SELECT R.a, S.d
  FROM R, S
 WHERE R.b = S.c AND S.e = 7
    
```

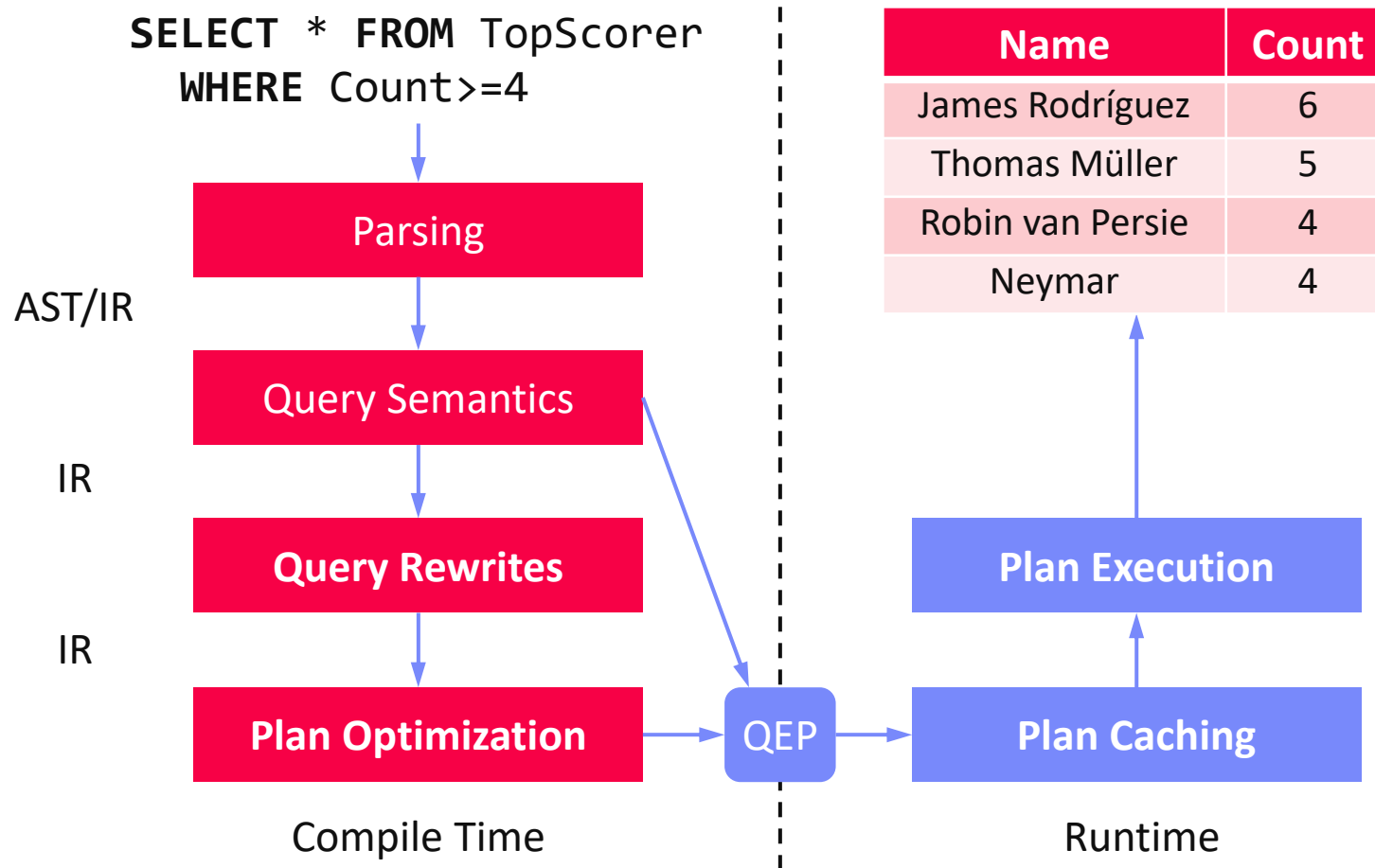


- Draw an optimized logical query tree for the above query in relational algebra by **eliminating the union** operation (3/100 points)



Plan Execution Strategies

Overview Query Processing



Overview Execution Strategies

- **Different execution strategies (processing models) with different pros/cons** (e.g., memory requirements, DAGs, efficiency, reuse)
- **#1 Iterator Model** (mostly row stores)
- **#2 Materialized Intermediates** (mostly column stores)
- **#3 Vectorized (Batched) Execution** (row/column stores)
- **#4 Query Compilation** (row/column stores)

High-level
overview,
details in
ADBS

Iterator Model

Scalable (small memory)

High CPI measures

Volcano Iterator Model

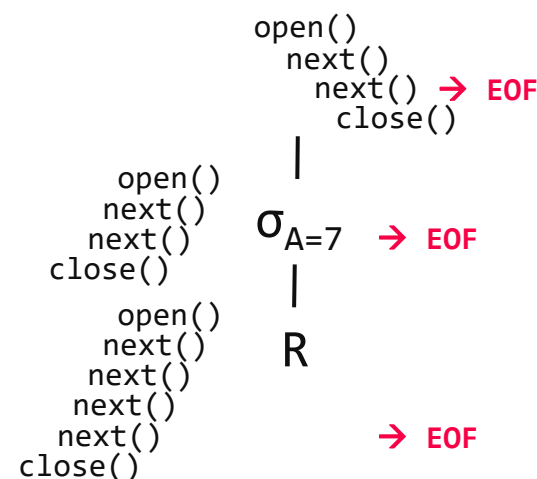
- Pipelined & no global knowledge
- **Open-Next-Close** (ONC) interface
- Query execution from root node (pull-based)

[Goetz Graefe: Volcano - An Extensible and Parallel Query Evaluation System. IEEE Trans. Knowl. Data Eng. 1994]



Example $\sigma_{A=7}(R)$

```
void open() { R.open(); }
void close() { R.close(); }
Record next() {
  while( (r = R.next()) != EOF )
    if( p(r) ) //A==7
      return r;
  return EOF;
}
```



Blocking Operators

- Sorting, grouping/aggregation, build-phase of (simple) hash joins

PostgreSQL: `Init()`,
`GetNext()`, `ReScan()`, `MarkPos()`,
`RestorePos()`, `End()`

Iterator Model – Predicate Evaluation

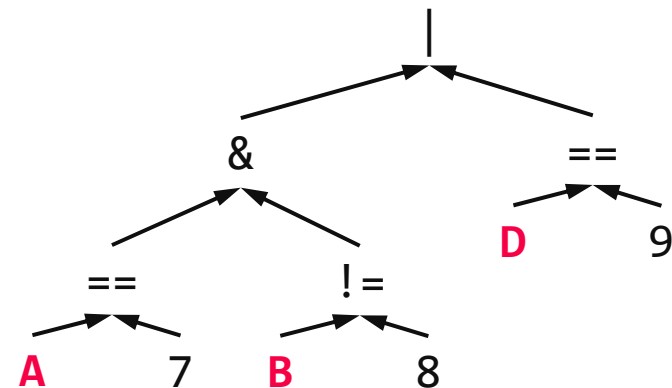
Operator Predicates

- Examples: arbitrary selection predicates and join conditions
- Operators parameterized **with in-memory expression trees/DAGs**
- Expression evaluation engine** (interpretation)

Example Selection σ

- $(A = 7 \wedge B \neq 8) \vee D = 9$

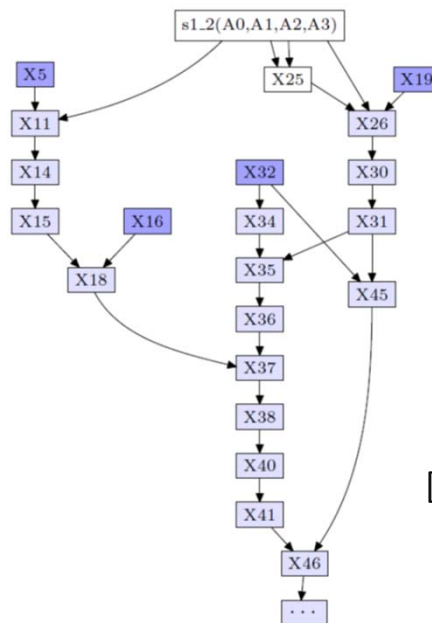
A	B	C	D
7	8	Product 1	10
14	8	Product 3	11
7	3	Product 7	7
3	3	Product 2	1



Materialized Intermediates (column-at-a-time)

```
SELECT count(DISTINCT o_orderkey)
FROM orders, lineitem
WHERE l_orderkey = o_orderkey
    AND o_orderdate >= date '1996-07-01'
    AND o_orderdate < date '1996-07-01'
        + interval '3' month
    AND l_returnflag = 'R';
```

- Column-oriented storage
- Efficient array operations
- DAG processing
- Reuse of intermediates
- Memory requirements
- Unnecessary read/write from and to memory



```
function user.s1_2(A0:date,A1:date,A2:int,A3:str):void;
  X5 := sql.bind("sys", "lineitem", "l_returnflag", 0);
  X11 := algebra.uselect(X5,A3);
  X14 := algebra.markT(X11,0@0);
  X15 := bat.reverse(X14);
  X16 := sql.bindIdxbat("sys", "lineitem", "l_orderkey_fkey");
  X18 := algebra.join(X15,X16);
  X19 := sql.bind("sys", "orders", "o_orderdate", 0);
  X25 := mtime.addmonths(A1,A2);
  X26 := algebra.select(X19,A0,X25,true,false);
  X30 := algebra.markT(X26,0@0);
  X31 := bat.reverse(X30);
  X32 := sql.bind("sys", "orders", "o_orderkey", 0);
  X34 := bat.mirror(X32);
  X35 := algebra.join(X31,X34);
  X36 := bat.reverse(X35);
  X37 := algebra.join(X18,X36);
  X38 := bat.reverse(X37);
  X40 := algebra.markT(X38,0@0);
  X41 := bat.reverse(X40);
  X45 := algebra.join(X31,X32);
  X46 := algebra.join(X41,X45);
  X49 := algebra.selectNotNil(X46);
  X50 := bat.reverse(X49);
  X51 := algebra.kunique(X50);
  X52 := bat.reverse(X51);
  X53 := aggr.count(X52);
  sql.exportValue(1,"sys.orders", "L1", " wrd", ,32,0,6,X53);
end s1_2;
```

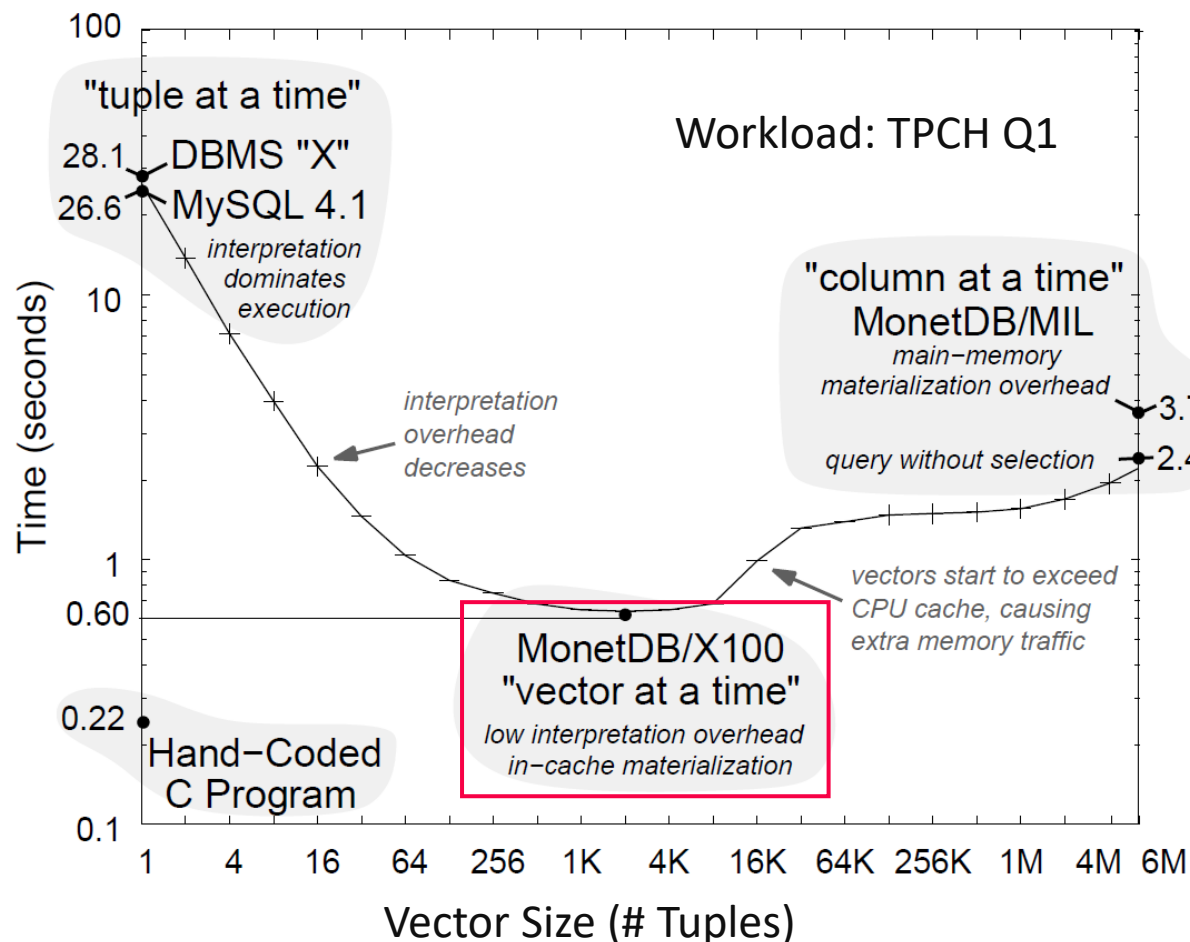
Binary Association Tables
(BATs:=OID/Val)

[Milena Ivanova, Martin L. Kersten, Niels J. Nes, Romulo Goncalves: An architecture for recycling intermediates in a column-store. **SIGMOD 2009**]



Vectorized Execution (vector-at-a-time)

- Idea: Pipelining of vectors (sub columns) s.t. vectors fit in CPU cache



Column-oriented storage
 Efficient array operations
 Memory/cache efficiency
 DAG processing
Reuse of intermediates



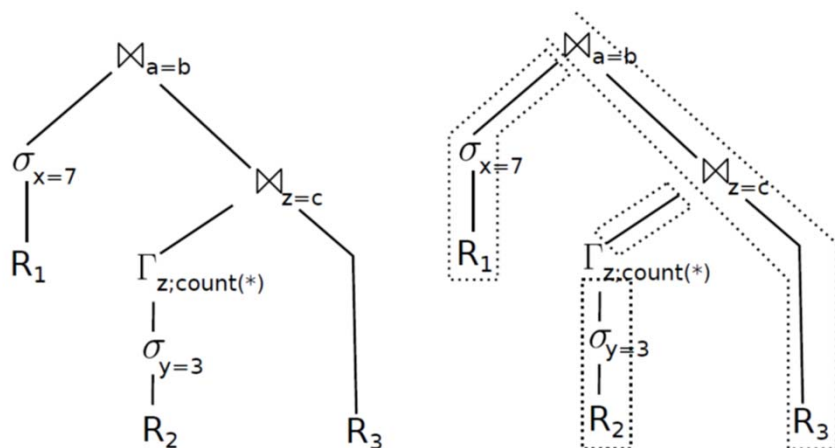
[Peter A. Boncz, Marcin Zukowski, Niels Nes: MonetDB/X100: Hyper-Pipelining Query Execution. CIDR 2005]

Query Compilation

- Idea: Data-centric, not op-centric processing + LLVM code generation

Operator Trees

(w/o and w/ pipeline boundaries)



Compiled Query

(conceptual, not LLVM)

```

initialize memory of  $\bowtie_{a=b}$ ,  $\bowtie_{c=z}$ , and  $\Gamma_z$ 
[
  for each tuple  $t$  in  $R_1$ 
    if  $t.x = 7$ 
      materialize  $t$  in hash table of  $\bowtie_{a=b}$ 
  for each tuple  $t$  in  $R_2$ 
    if  $t.y = 3$ 
      aggregate  $t$  in hash table of  $\Gamma_z$ 
  for each tuple  $t$  in  $\Gamma_z$ 
    materialize  $t$  in hash table of  $\bowtie_{z=c}$ 
  for each tuple  $t_3$  in  $R_3$ 
    for each match  $t_2$  in  $\bowtie_{z=c}[t_3.c]$ 
      for each match  $t_1$  in  $\bowtie_{a=b}[t_3.b]$ 
        output  $t_1 \circ t_2 \circ t_3$ 
]
    
```



[Thomas Neumann: Efficiently Compiling Efficient Query Plans for Modern Hardware. **PVLDB 2011**]

Physical Plan Operators

Overview Plan Operators

- Multiple Physical Operators

- Different physical operators for different data and query characteristics
- Physical operators can have vastly different costs

- Examples (supported in most DBMS)

Logical Plan Operators	Selection $\sigma_p(R)$	Projection $\pi_A(R)$	Grouping $\gamma_{G:agg(A)}(R)$	Join $R \bowtie_{R.a=S.b} S$
Physical Plan Operators	TableScan IndexScan ALL	ALL	SortGB HashGB	NestedLoopJN SortMergeJN HashJN
	Lecture 07			This Lecture Exercise 3

Nested Loop Join

Overview

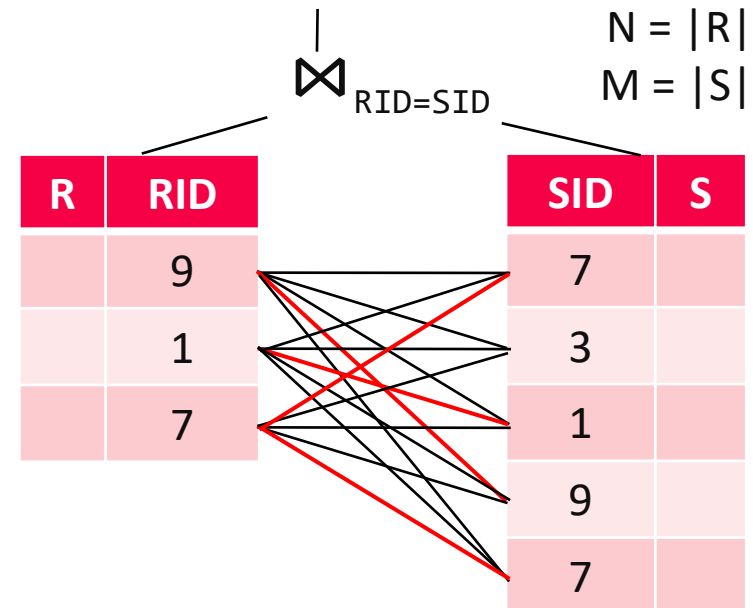
- **Most general join operator** (no order, no indexes, arbitrary predicates θ)
- **Poor asymptotic behavior** (very slow)

Algorithm (pseudo code)

```

for each s in S
  for each r in R
    if( r.RID  $\theta$  s.SID )
      emit concat( r, s )
  
```

How to implement **next()**?



Complexity

- Complexity: Time: $O(N * M)$, Space: $O(1)$
- Pick smaller table as inner if it fits entirely in memory (buffer pool)

Block Nested Loop / Index Nested Loop Joins

Block Nested Loop Join

- Avoid I/O by blocked data access
- Read blocks of b_R and b_S R and S pages
- Complexity unchanged but potentially much fewer scans

```

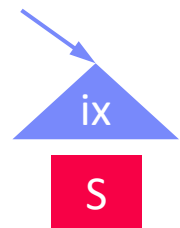
for each block  $b_R$  in R
  for each block  $b_S$  in S
    for each  $r$  in  $b_R$ 
      for each  $s$  in  $b_S$ 
        if(  $r.RID \theta s.SID$  )
          emit concat( $r, s$ )
  
```

Index Nested Loop Join

- Use index to locate qualifying tuples
($=$, $>=$, $>$, $<=$, $<$)
- Complexity (for equivalence predicates):
Time: $O(N * \log M)$, Space: $O(1)$

```

for each  $r$  in R
  for each  $s$  in  $S.IX(\theta, r.RID)$ 
    emit concat( $r, s$ )
  
```



Sort-Merge Join

Overview

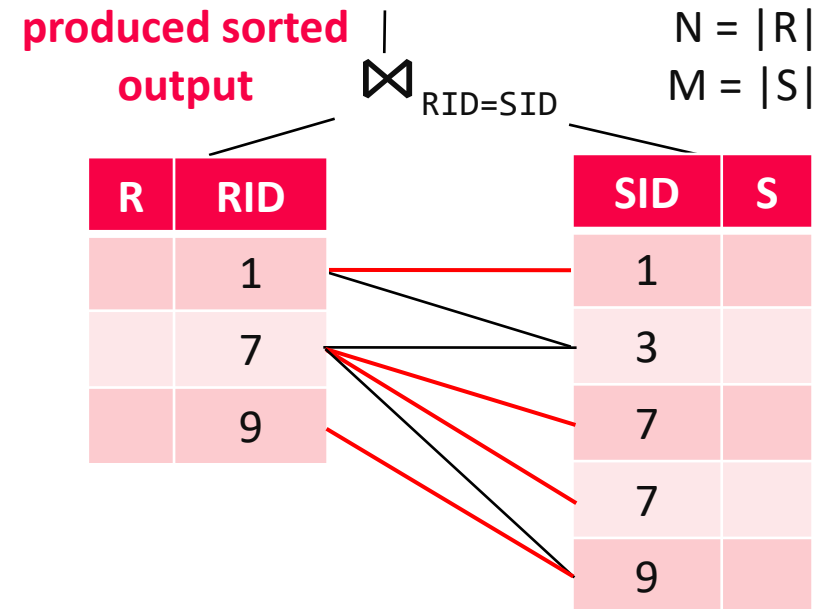
- **Sort Phase:** sort the input tables R and S (w/ external sort algorithm)
- **Merge Phase:** step-wise merge with lineage scan

Algorithm (Merge, PK-FK)

```

Record next() {
  while( curR!=EOF && curS!=EOF ) {
    if( curR.RID < curS.SID )
      curR = R.next();
    else if( curR.RID > curS.SID )
      curS = S.next();
    else if( curR.RID == curS.SID ) {
      t = concat(curR, curS);
      curS = S.next(); //FK side
      return t;
    }
  }
  return EOF;
}

```



Complexity

- Time (unsorted vs sorted): $O(N \log N + M \log M)$ vs $O(N + M)$
- Space (unsorted vs sorted): $O(N + M)$ vs $O(1)$

Hash Join

Overview

- **Build Phase:** read table S and build a hash table H_S over join key
- **Probe Phase:** read table R and probe H_S with the join key

Algorithm (Build+Probe, PK-FK)

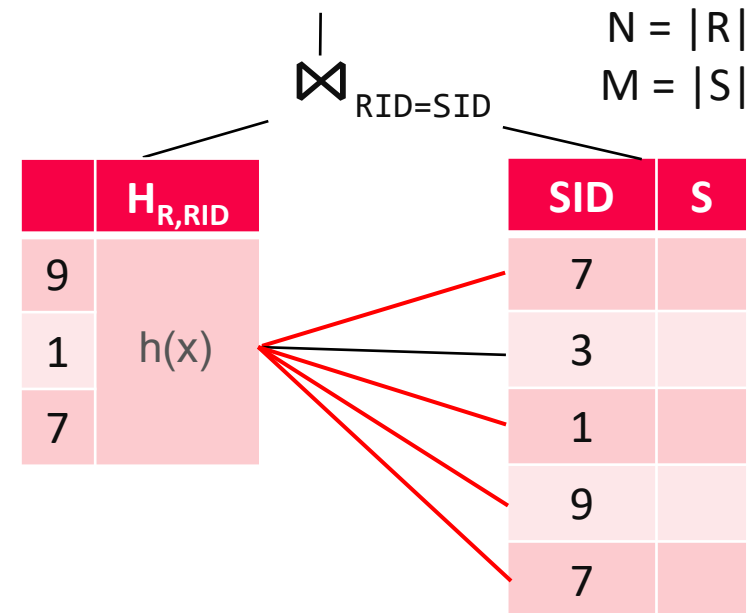
```

Record next() {
  // build phase (first call)
  while( (r = R.next()) != EOF )
    Hr.put(r.RID, r);

  // probe phase
  while( (s = S.next()) != EOF )
    if( Hr.containsKey(s.SID) )
      return concat(Hr.get(s.SID), s);

  return EOF;
}

```



Complexity

- Time: $O(N + M)$, Space: $O(N)$
- Classic hashing: p in-memory partitions of H_r w/ p scans of R and S

Conclusions and Q&A

- **Summary**
 - Query rewriting and query optimization
 - Query processing and physical operators

- **Exercise 2 Reminder**
 - Submission deadline: **Nov 26 11.59pm** (+ max 7 late days)
 - **Total points \geq 50%, but crucial to submit**

- **Next Lectures**
 - Dec 02: **09 Transaction Processing and Concurrency**