



Architecture of DB Systems 04 Index Structures and Partitioning

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Last update: Oct 28, 2020





Announcements/Org

#1 Video Recording

Link in TeachCenter & TUbe (lectures will be public)



Optional attendance (independent of COVID)

#2 COVID-19 Restrictions (HS i5)

Corona Traffic Light: Orange

max 18/74

Max 25% room capacity (TC registrations)

#3 Programming Projects

- Updated Project Setup.zip, news group will be set up
- Requirements
 - Test suite must pass, no test cheating and gaming
 - Min performance target: T(SUT) < 4 * T(ref_impl) tested on 32 indexes/threads, different benchmarks and sizes</p>
 - Deadline: Thu Jan 21 11.59pm





Agenda

- Overview Access Methods
- Index Structures
- Partitioning and Pruning
- Adaptive and Learned Access Methods

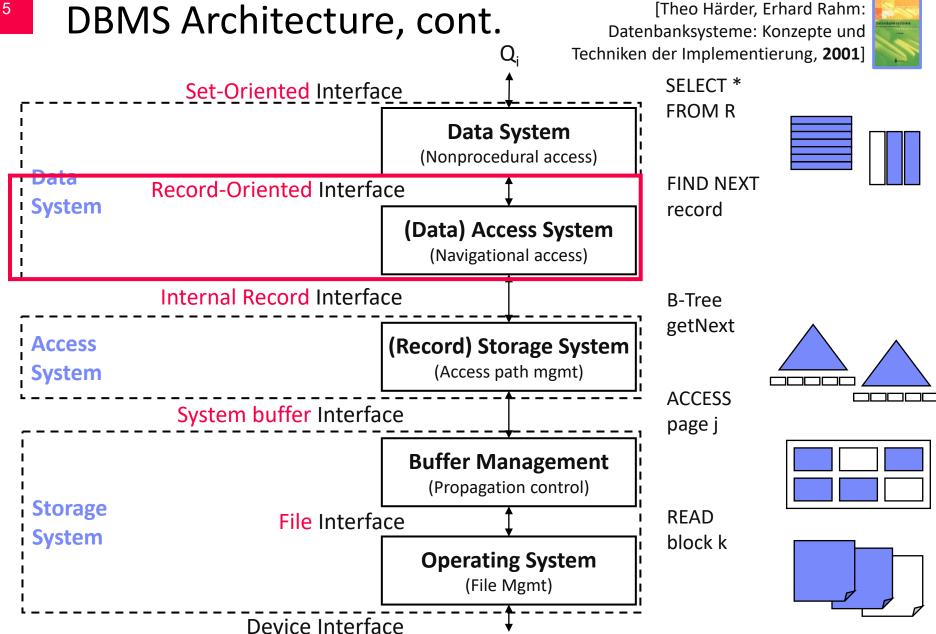




Overview Access Methods







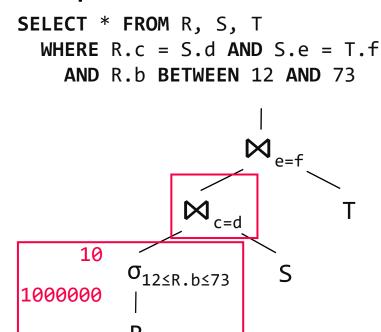


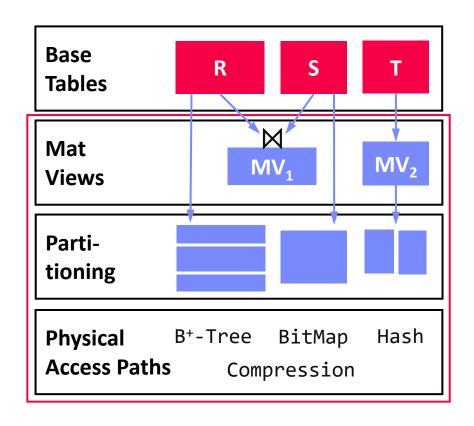
Access Methods and Physical Design

Performance Tuning via Physical Design

- Select physical data structures for relational schema and query workload
- #1: User-level, manual physical design by DBA (database administrator)
- #2: User/system-level automatic physical design via advisor tools

Example



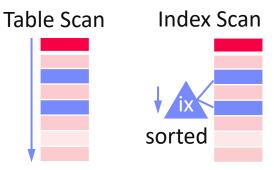




Overview Index Structures

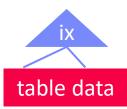
Table Scan vs Index Scan

- For highly selective predicates, index scan asymptotically much better than table scan
- Index scan higher overhead (~5% break even)
 - IXScan → TID-Sort → TID-Fetch
 - Multi-column predicates: TID-list intersection

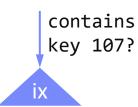


Use Cases for Indexes

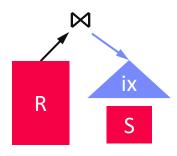
Lookups / Range Scans



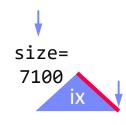
Unique Constraints



Index Nested Loop Joins



Aggregates (count, min/max)



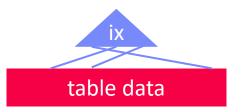




Additional Terminology

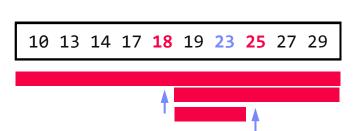
Create Index

- Create a secondary (nonclustered) index on a set of attributes
- Clustered: tuples sorted by index
- Non-clustered: sorted attribute with tuple references
- Can specify uniqueness, order, and indexing method
- PostgreSQL methods: <u>btree</u>, hash, gist, and gin



Binary Search

- pos = binarySearch(data,key=23)
- Given sorted data, find key position (insert position if non-existing)
- k-ary search for SIMD data-parallelism
- Interpolation search: probe expected pos in key range (e.g., search([1:10000], 9700))



CREATE INDEX ixStudiname

ON Students **USING** btree

(Lname ASC NULLS FIRST);





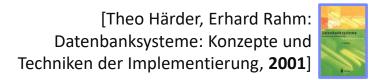
Index Structures

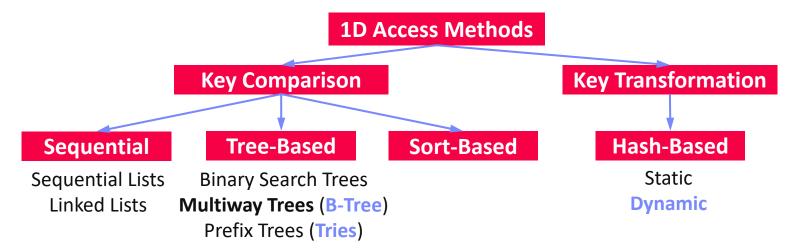




Classification of Index Structures

1D Access Methods





ND Access Methods

- Linearization of ND key space + 1D indexing (Z order, Gray code, Hilbert curve)
- Multi-dimensional trees and hashing (e.g., UB tree, k-d tree, gridfile)
- Spatial index structures (e.g., R tree)





B-Tree Overview

[Rudolf Bayer, Edward M. McCreight: Organization and Maintenance of Large Ordered Indices. Acta Inf. (1) 1972]



History B-Tree

- Bayer and McCreight 1972, Block-based, Balanced, Boeing Labs
- Multiway tree (node size = page size); designed for DBMS
- Extensions: B+-Tree/B*-Tree (data only in leafs, double-linked leaf nodes)

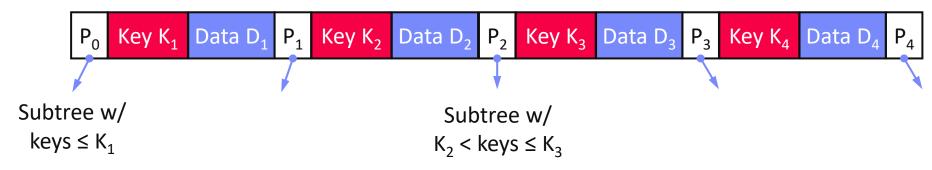
Definition B-Tree (k, h)

- All paths from root to leafs have equal length h
 - . -
- $\lceil \log_{2k+1}(n+1) \rceil \le h \le \left| \log_{k+1}\left(\frac{n+1}{2}\right) \right| + 1$
- All nodes (except root) have [k, 2k] key entries

All nodes adhere to max constraints

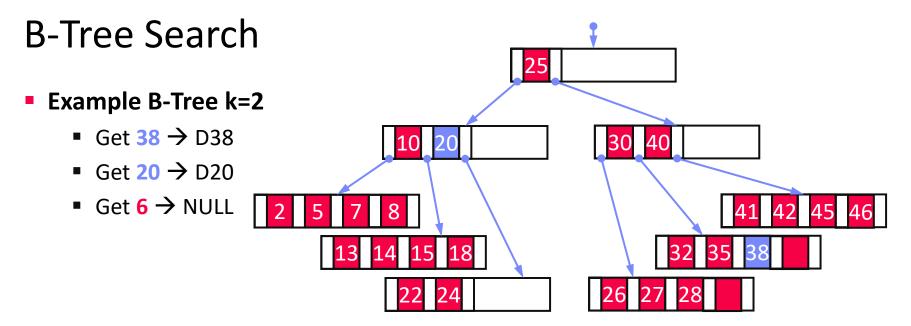
- All nodes (except root, leafs) have [k+1, 2k+1] successors
- Data is a record or a reference to the record (RID)

k=2









Lookup Q_K within a node

- Scan / binary search keys for Q_K, if K_i=Q_K, return D_i
- If node does not contain key
 - If leaf node, abort search w/ NULL (not found), otherwise
 - Decent into subtree Pi with $K_i < Q_K \le K_{i+1}$

Range Scan Q_{L<K<U}

■ Lookup Q_L and call next K while K<Q_U (keep current position and node stack)





B-Tree Insert

Basic Insertion Approach

- Always insert into leaf nodes!
- Find position similar to lookup, insert and maintain sorted order
- If node overflows (exceeds 2k entries) → node splitting

Node Splitting Approach

Split the 2k+1 entries into two leaf nodes

Left node: first k entries

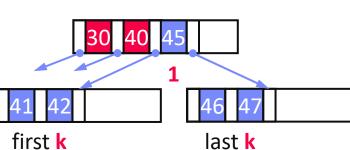
Right node: last k entries

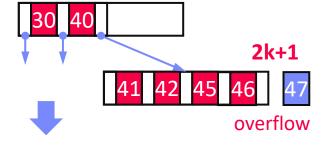
(k+1)th entry inserted into parent node

→ can cause recursive splitting

Special case: root split (h++)











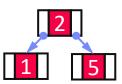
B-Tree Insert, cont. (Example w/ k=1)

Insert 1

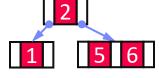
1

- Insert 5
- 1 5

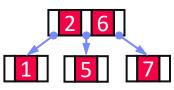
Insert 2 (split)



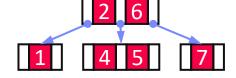
Insert 6



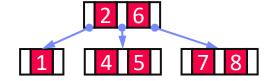
Insert 7 (split)



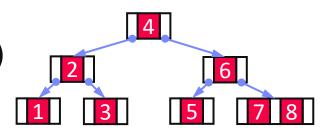
Insert 4



Insert 8



Insert 3 (2x split)



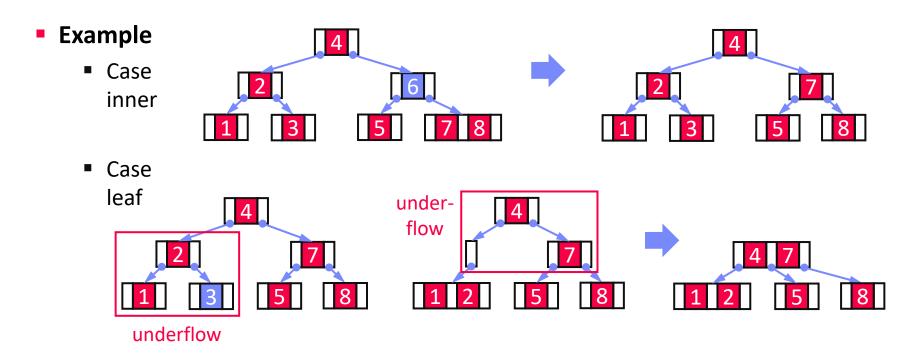




B-Tree Delete

Basic Deletion Approach

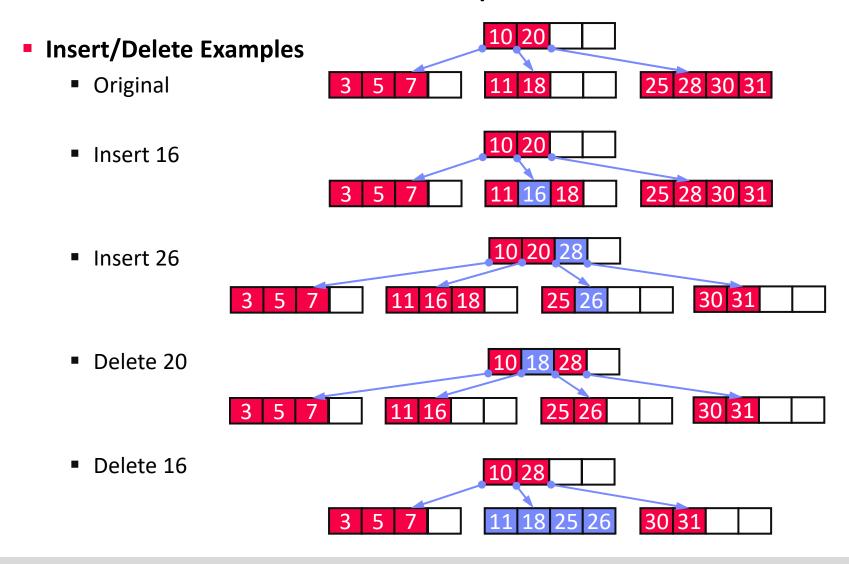
- Lookup deletion key, abort if non-existing
- Case inner node: move entry from fullest successor node into position
- Case leaf node: if underflows (<k entries) → merge w/ sibling</p>







B-Tree Insert and Delete w/ k=2





B-tree – Advanced Aspects

[Goetz Graefe: Modern B-Tree Techniques. Found. Trends Databases 3(4): 203-402, 2011]



Variable-Length Fields

- In-page slot-array to variable length fields → direct lookup
- With fixed page size, no guarantees on min/max entries
- Various approaches: overflow pages, pick separators during bulk loading

Concurrent Access

- DB locks: only leaf nodes for B+ tree in practice at value/value ranges
- Concurrent threads require page latching (parent-child)

Duplicate Keys

- #1 use prefix truncation for compression → store common prefix once)
- #2 concatenate key-TID for unique lockups w/ O(log N)
- Duplicate records as replicates or once w/ counter





Other In-Memory Trees

Balanced Binary Trees

- Red-Black Tree, AVL Tree (left/right height diff 1)
- T tree (combines pros of AVL and B trees)



[G. M. Adel'son-Vel'skii and E. M. Landis: An algorithm for the organization of information, Soviet Mathematics Doklady, 3, 1962]

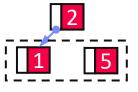


[Tobin J. Lehman, Michael J. Carey: A Study of Index Structures for Main Memory Database Management Systems. **VLDB 1986**]



CSB+-Tree

- Align node size to cache line (64B)
- Reduce pointers via node groups
- More keys, higher fan-out, at cost of slower insert



[Jun Rao, Kenneth A. Ross: Making B+-Trees Cache Conscious in Main Memory. SIGMOD 2000]



Skip Lists

- Linked list with multiple levels
- Fraction p w/ level i pointers



[William Pugh: Skip Lists: A Probabilistic Alternative to Balanced Trees. **CACM 1990**]







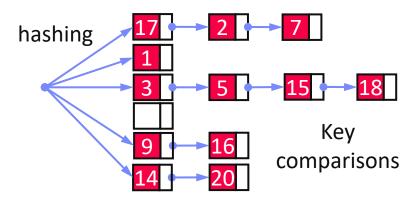
Hashing Overview

Static vs Dynamic Hashing

- Hash table of buckets B, compute h=hash(key), find bucket B[h mod |B|]
- Static: pre-allocation of buckets, over- and under-provisioning (open addressing: linear probe, robin hood, cuckoo)
- Dynamic: extend as needed (chained bucket, extendible, linear hashing)

Chained Bucket Hashing

- Handle hash collisions via overflow list of linked buckets
- Reorganization if fill factor reached
- On disk: buckets are pages



Common Hash Functions

- MurmurHash 2, MurmurHash 3, Jenkins, CRC
- Google CityHash, Google FarmHash, Facebook XXHash3 (http://cyan4973.github.io/xxHash/)

[Andy Palvo: Database Systems – Hash Tables, CMU Lecture, **2019**]







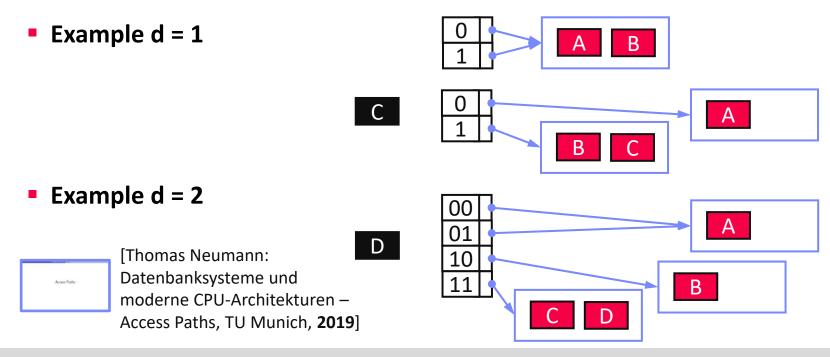
Extendible Hashing

[Ronald Fagin, Jürg Nievergelt, Nicholas Pippenger, H. Raymond Strong: Extendible Hashing - A Fast Access Method for Dynamic Files. **TODS 4(3), 1979**]



Overview

- Dynamic resizing on demand, w/o rehashing/reassigning tuples to pages
- h=hash(key), use d bits and directory of 2^d entries
 (with max table size, then bucket chaining)
- Directory entries point to buckets, multiple refs to one bucket possible







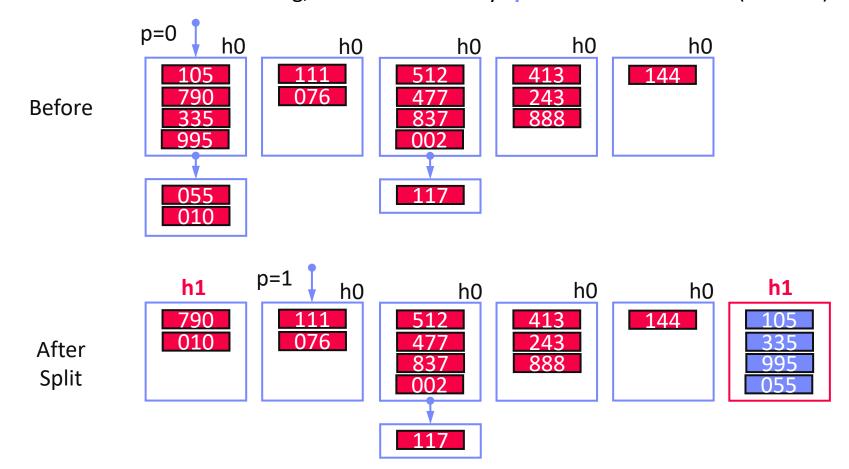
Linear Hashing

[Theo Härder, Erhard Rahm: Datenbanksysteme: Konzepte und Techniken der Implementierung, **2001**]



Overview

- Improved Extensible Hashing scheme, w/o exponential directory growth
- First start chaining, then incrementally split individual buckets (in order)





Overview Prefix Trees (Tries)

Overview

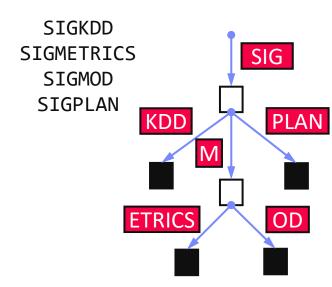
- From information retrieval, mostly for string indexing
- Trie: "A tree for storing strings in which there is one node for every common prefix. The strings are stored in extra leaf nodes." (NIST DADS)

PATRICIA Trie

Extended binary (character-level)
 trie, with compressed substrings



[Donald R. Morrison: PATRICIA - Practical Algorithm To Retrieve Information Coded in Alphanumeric. J. ACM 15(4) 1968]



Variants

 Radix Tree, key alteration radix tree (Kart), digital search trees





Generalized Prefix Tree

[Matthias Boehm et al: Efficient In-Memory Indexing with Generalized **Prefix Trees. BTW 2011**

0000 0000 0110 1011

INSERT key=107, payload="value3"

kev = 107

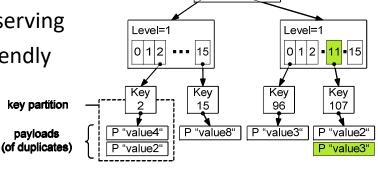


Generalized Prefix Tree (IXByte)

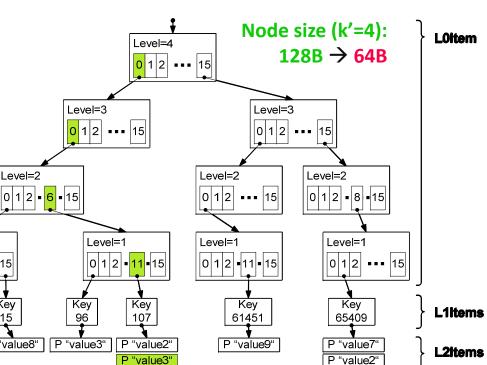
- Arbitrary data types (byte sequences)
- Variable prefix length k'
- Node size: $s = 2^{k'}$ references
- Fixed maximum height h = k/k'
- Secondary index structure

Characteristics

- Partitioned data structure
- Deterministic paths
- Order-preserving
- Update-friendly
- Trie **Expansion** & Bypass



Level=2





Node Types



Adaptive Radix Trees

[Viktor Leis, Alfons Kemper, Thomas Neumann: The adaptive radix tree: ARTful Indexing for Main-Memory Databases. ICDE 2013

S=1

32MB

32

tree height

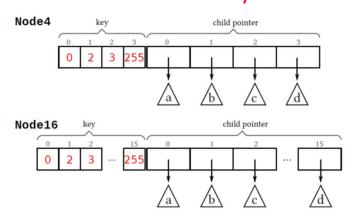
16 -

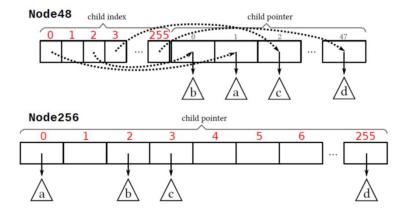


Motivation and Overview

- Small trie height/high fan-out, but with low space overhead
- Prefix $k'=8 \rightarrow 256$ children
- Adaptive nodes 4, 16, 48, 256 entries
- Lazy expansion and path compression

Linear/binary 256 element arrays of search for keys indexes / child pointers





128MB 512MB

2GB

space consumption (log scale)

8GB

32GB





Hybrid Prefix Trees

	Binary	B-Tree	CSB-Tree	Hash	T-Tree	Trie
Prefix Hash Tree '70				X		X
Prefix B-Tree '77		X				X
Ternary Search Tree '97	X					X
Partial Keys '01		Χ			X	X
Burst-Trie '02	X	X	X	X	X	X
HAT-Trie '07				X		X
J+-Tree '09		X			X	X
CS-Prefix Tree '09			X			Х
SuRF '18				X		X



Partitioning and Pruning

Coarse-grained Table Partitioning
Fine-grained Physical Partitioning and Sketching





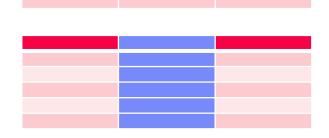
Overview Partitioning Strategies

Horizontal Partitioning

Relation partitioning into disjoint subsets

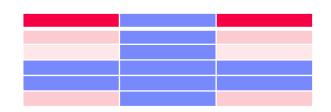
Vertical Partitioning

 Partitioning of attributes with similar access pattern



Hybrid Partitioning

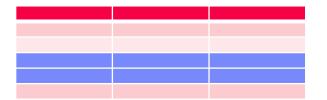
 Combination of horizontal and vertical fragmentation (hierarchical partitioning)



Derived Horizontal Partitioning







Physical Partitioning Schemes

Hash Partitioning, Round-Robin, Radix Partitioning, etc



Correctness Properties

#1 Completeness

- $R \rightarrow R_1, R_2, ..., R_n$ (Relation R is partitioned into *n* fragments)
- Each item from R must be included in at least one fragment

#2 Reconstruction

- $R \rightarrow R_1, R_2, ..., R_n$ (Relation R is partitioned into *n* fragments)
- Exact reconstruction of fragments must be possible

#3 Disjointness

- $R \rightarrow R_1, R_2, ..., R_n$ (Relation R is partitioned into n fragments)
- $R_i \cap R_j = \emptyset \ (1 \le i, j \le n; \ i \ne j)$

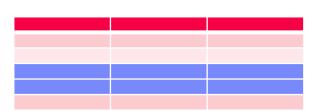




Horizontal Partitioning

Row Partitioning into n Fragments R_i

- Complete, disjoint, reconstructable
- Schema of fragments is equivalent to schema of base relation



Partitioning

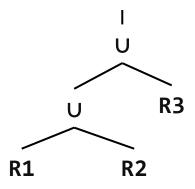
- Split table by n selection predicates P_i
 (partitioning predicate) on attributes of R
- Beware of attribute domain and skew

$$R_i = \sigma_{P_i}(R)$$

$$(1 \le i \le n)$$

Reconstruction

- Union of all fragments
- Bag semantics, but no duplicates across partitions



$$R = \bigcup_{1 \le i \le n} R_i$$

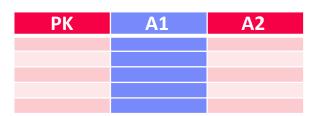




A1

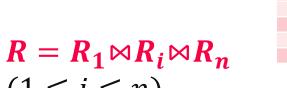
Vertical Fragmentation

- Column Partitioning into n Fragments Ri
 - Complete, reconstructable, but not disjoint (primary key for reconstruction via join)
 - Completeness: each attribute must be included in at least one fragment



- Partitioning
 - Partitioning via projection
 - Redundancy of primary key

R_i	=	$\pi_{PK,A_i}(R$	うし
		$i \leq n$	



			. •
R	eco	nstri	uction

■ Natural join over primary key
$$(1 \le i \le n)$$

$$R = R_1 \bowtie R_i \bowtie R_n \bowtie / R_i = \cup R_{ij}$$

 $\Rightarrow R = \cup R_i \bowtie / R_i = R_{1i} \bowtie R_{ii} \bowtie R_{ni}$



Derived Horizontal Fragmentation

- Row Partitioning R into n fragements
 R_i, with partitioning predicate on S
- Austria
- Potentially complete (not guaranteed),
 restructable, disjoint
- Foreign key / primary key relationship determines correctness

Partitioning

- Selection on independent relation S
- Semi-join with dependent relation R to select partition R_i

$$R_{i} = R \ltimes S_{i} = R \ltimes \sigma_{P_{i}}(S)$$
$$= \pi_{R,*} \left(R \bowtie \sigma_{P_{i}}(S) \right)$$

Reconstruction

- Equivalent to horizontal partitioning
- Union of all fragments

$$R = \bigcup_{1 \le i \le n} R_i$$





Exploiting Table Partitioning

Partitioning and query rewriting

- #1 Manual partitioning and rewriting
- #2 Automatic rewriting (spec. partitioning)
- #3 Automatic partitioning and rewriting

Example PostgreSQL (#2)

```
CREATE TABLE Squad(
    JNum INT PRIMARY KEY,
    Pos CHAR(2) NOT NULL,
    Name VARCHAR(256)
) PARTITION BY RANGE(JNum);

CREATE TABLE Squad10 PARTITION OF Squad
    FOR VALUES FROM (1) TO (10);

CREATE TABLE Squad20 PARTITION OF Squad
    FOR VALUES FROM (10) TO (20);

CREATE TABLE Squad24 PARTITION OF Squad
    FOR VALUES FROM (20) TO (24);
```

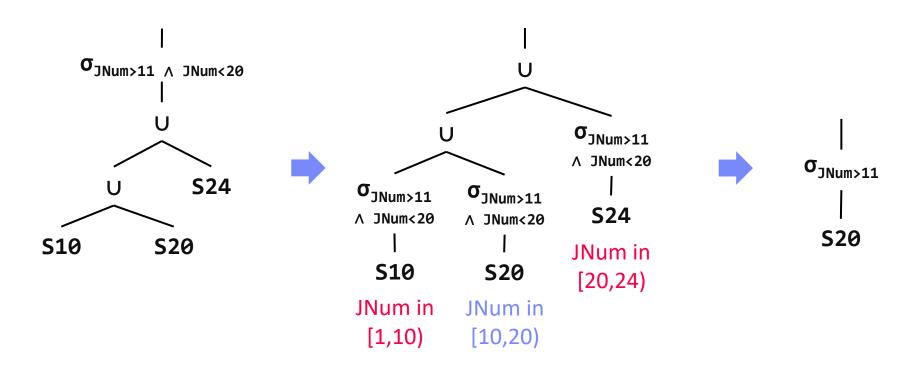
J#	Pos	Name				
1	GK	Manuel Neuer				
12	GK	Ron-Robert Zieler				
22	GK	Roman Weidenfeller				
2	DF	Kevin Großkreutz				
4	DF	Benedikt Höwedes				
5	DF	Mats Hummels				
15	DF	Erik Durm				
16	DF	Philipp Lahm				
17	DF	Per Mertesacker				
20	DF	Jérôme Boateng				
3	MF	Matthias Ginter				
6	MF	Sami Khedira				
7	MF	Bastian Schweinsteiger				
8	MF	Mesut Özil				
9	MF	André Schürrle				
13	MF	Thomas Müller				
14	MF	Julian Draxler				
18	MF	Toni Kroos				
19	MF	Mario Götze				
21	MF	Marco Reus				
23	MF	Christoph Kramer				
10	FW	Lukas Podolski				
11	FW	Miroslav Klose				



Exploiting Table Partitioning, cont.

Example, cont.

SELECT * FROM Squad
WHERE JNum > 11 AND JNum < 20







Zone Maps

[Guido Moerkotte: Small Materialized Aggregates: A Light Weight Index Structure for Data Warehousing. **VLDB 1998**]



- Small Materialized Aggregates (SMA)
 - Data stored in zones (pages, blocks, or partitions)
 - Maintain SMA (e.g., min, max, count, sum) as summary per zone
 - Global vs local storage, eager vs lazy maintenance on updates

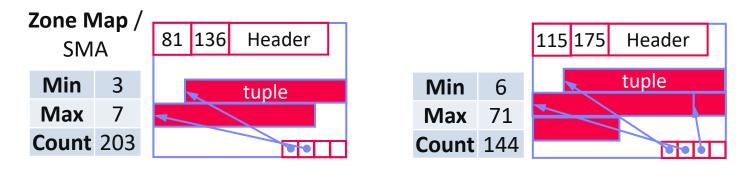


Table Scan for $\sigma_{B=10}(R)$

Query Processing

- Partition pruning for selection predicates
- Precomputed partial aggregates (see materialized views)





Column Imprints

[Lefteris Sidirourgos, Martin L. Kersten: Column imprints: a secondary index structure. **SIGMOD 2013**]

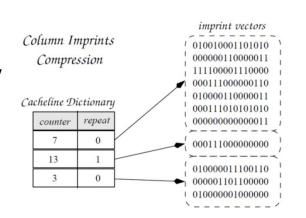


Column Imprints

- Zone = cache line (64 Byte)
- Column imprint = union of one-hot vectors
- Sampled histogram → bins (max 64 bins)

Compression

CL Dictionary (next x CLs, repeat flag)



	column	Zone Map		$\mathcal{B}it\mathcal{M}ap$				p	Column Imprint	
e	1		1	0	0	0	0	0	0:0	
cacheline	8	[1, 8]	0	0	0	0	0	0	0:1	10010001
; cac	4		0	0	0	1	0	0	0:0	
эe	6		0	0	0	0	0	1	0:0	
cacheline	7	[1, 6]	0	0	0	0	0	0	1 0	10000110
; cac	1		1	0	0	0	0	0	0:0	
эс	4		0	0	0	1	0	0	0:0	
cacheline	7	[3, 7]	0	0	0	0	0	0	1:0	00110010
; cac	3		0	:0	1	0	0	0	0 0	
<u>ə</u>	2		0	1	0	0	0	0	0:0	
cacheline	5	[2, 6]	0	0	0	0	1	0	0:0	01001100
cac	6		0	0:	0	0	0	1	0:0	
9	8		0	0	0	0	0	0	0 : 1	
cacheline	2	[1, 8]	0	1	0	0	0	0	0:0	11000001
cac	1		1	0	0	0	0	0	0 0	

Query Processing

- Cacheline pruning for selection predicates (point, range)
- imprint & predicate (predicate w/ potentially many bits for ranges)





Adaptive and Learned Access Methods





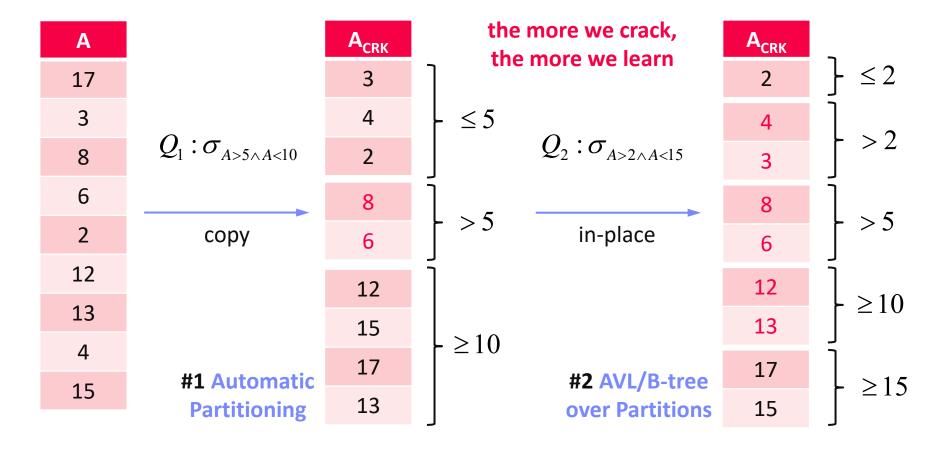
Database Cracking

 Core Idea: Queries trigger physical reorganization (partitioning and indexing) [Pedro Holanda et al: Progressive Indexes: Indexing for Interactive Data Analysis. **PVLDB 2019**]



[Stratos Idreos, Martin L. Kersten, Stefan Manegold: Database Cracking. **CIDR 2007**]





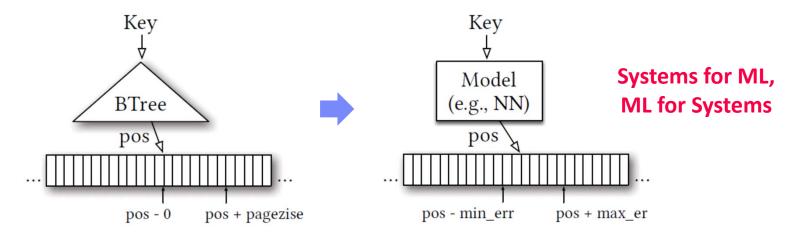


Learned Index Structures

- A Case For Learned Index Structures
 - Sorted data array, predict position of key
 - Hierarchy of simple models (stages models)
- [Tim Kraska, Alex Beutel, Ed H. Chi, Jeffrey Dean, Neoklis Polyzotis: The Case for Learned Index Structures. SIGMOD 2018]



Tries to approximate the CDF similar to interpolation search (uniform data)



Follow-up Work on SageDBMS



[Tim Kraska, Mohammad Alizadeh, Alex Beutel, Ed H. Chi, Ani Kristo, Guillaume Leclerc, Samuel Madden, Hongzi Mao, Vikram Nathan: SageDB: A Learned Database System. CIDR 2019]





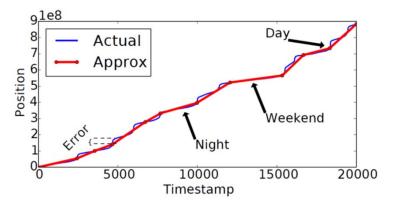
Learned Index Structures, cont.

FITing-Tree

- Adapt to underlying data and patterns
- Piecewise linear functions
- Maximum pos error guarantees
- Segment pages w/ free space

[Alex Galakatos, Michael Markovitch, Carsten Binnig, Rodrigo Fonseca, Tim Kraska: FITing-Tree: A Data-aware Index Structure. **SIGMOD 2019**]





PGM-index

- Piecewise geometric model index
- Recursive, compressed segment tree

[Paolo Ferragina, Giorgio Vinciguerra: The PGM-index: a fully-dynamic compressed learned index with provable worst-case bounds. PVLDB 13(8) 2020]



RadixSpline

 Lookup table to spline points, selected w/ max error guarantee [Andreas Kipf, Ryan Marcus, Alexander van Renen, Mihail Stoian, Alfons Kemper, Tim Kraska, Thomas Neumann: RadixSpline: a single-pass learned index. aiDM@SIGMOD 2020]







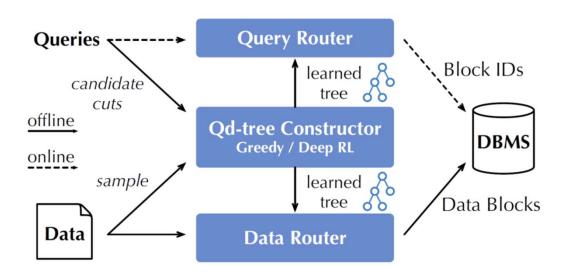
Learned Partitioning Schemes

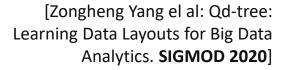
Query-Data Routing Tree (qd-Tree)

- Binary decision tree, with data blocks at leaf nodes (min size constraint)
- Given dataset, and workload,
 find tree that minimized number of accessed tuples
- Deep reinforcement learning

Query Processing

 Get list of blocks that need to be evaluated











Summary and Q&A

- Overview Access Methods
- Index Structures
- Partitioning and Pruning
- Adaptive and Learned Access Methods
- Programming Projects
 - Initial test suite, benchmark, make file, and reference implementation
 - Start your own implementation in next weeks
- Next Lectures (Part A)
 - 05 Compression Techniques [Nov 04]

